## Substantive <br> Knowledge

| Topic | Substantive Knowledge <br> This is the specific, factual content for the topic, which should be connected into a careful sequence of learning. | Disciplinary Knowledge (Skills) <br> This is the action taken within a particular topic in order to gain substantive knowledge. | Assessment Opportunities <br> What assessments will be used to measure student progress? |
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| Introduction to Maths at Blue Coat | - 4 operations with positive and negative integers <br> - Rounding and estimating <br> - Area and perimeter of rectangles and triangles <br> - Units of measure <br> - Graphs, coordinates, axes scales <br> - Scatter diagrams <br> - Use of scientific calculators <br> - Powers and roots <br> - Function machines <br> - Data analysis: averages, charts and diagrams <br> - Basic angles facts including 'perpendicular' | - Addition, subtraction, multiplication and division of positive and negative integers, including mental and written strategies <br> - Round to whole numbers and decimal places. <br> - Use estimates to check appropriateness of answers <br> - Calculate area and perimeter of rectangles and triangles <br> - Work with different units including conversions, and selecting appropriate units <br> - Plot coordinates and working with different scales on axes <br> - Identify issues with "bad graphs" <br> - Read from scatter diagrams and lines of best fit <br> - Use scientific calculators to accurately answer problems including how to use powers, roots, brackets, fractions, and mixed numbers <br> - Find powers and roots of numbers <br> - Use and create function machines <br> - Calculate averages and possible values of the set of data given summary statistics <br> - Read from bar charts, pictograms, and pie charts <br> - Working with angles and angle reasoning (but not parallel lines), including angles around a point, on a straight line, in a triangle, in a quadrilateral | - Teacher diagnostic questioning <br> - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 1 test <br> - End of year assessments |


|  |  | - Understanding and using the word perpendicular |  |
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| Number | - Order of operations (BIDMAS) <br> - Directed number <br> - 4 operations with decimals, fractions, and mixed numbers <br> - Reciprocals <br> - Converting between fractions, mixed numbers, decimals and percentages <br> - Percentages | - Apply the correct order of operations (BIDMAS) and understand that the division and multiplication are the same level and are completed left to right, and analogously for addition and subtraction <br> - Addition, subtraction, multiplication and division of decimals, fractions and mixed numbers <br> - Find the reciprocal of a number and recognise the product of a number and its reciprocal makes 1 <br> - Convert between fractions, mixed numbers, decimals and percentages, and use this skill to compare proportions and answer complex numerical problems (including fractions that lead to recurring decimals) <br> - Percentage of an amount including percentages greater than 100\%, percentage increase and decrease, percentage change/error | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 1 test <br> - End of year assessments <br> - PQWC |
| Angles | - Angle rules for lines, triangles and quadrilaterals <br> - Angle definitions for parallel lines <br> - Tessellation | - Understand perpendicular means at a right angle/ $90^{\circ}$ <br> - Use angles around a point, angles on a straight line, angles in a triangle, and angles in a quadrilateral <br> - Use rules for alternate, corresponding, vertically opposite, and co-interior angles in parallel lines <br> - Use special properties of triangles and quadrilaterals to answer problems such as the base angles in an isosceles triangle being equal <br> - Solve geometrical problems using correct terminology <br> - Understand what tessellation is and why some shapes tessellate | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 2 test <br> - End of year assessments <br> - PQWC |
| Indices | - Laws of indices | - Use the rules of indices for multiplication, division, and brackets | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 2 test <br> - End of year assessments <br> - PQWC |


| Algebra | - Algebra vocabulary <br> - Collect like terms <br> - Substitution <br> - Solve linear equations <br> - Multiply a single term over a bracket <br> - Factorise a single term from an expression | - Use letter symbols to represent unknown numbers or variables <br> - Know the meanings of term, expression, equation and formula <br> - Know and use the order of operations and understand that algebra follow the same conventions and order as arithmetic <br> - Simplify linear algebraic expressions by collect like terms <br> - Substitute numbers into algebraic expressions and formulae to solve problems <br> - Construct and solve simple linear equations with integer coefficients <br> - Multiply a single term over a bracket <br> - Factorise algebraic expressions by finding a single common term | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 2 test <br> - End of year assessments <br> - PQWC |
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| Real Life Graphs | - Real life graphs <br> - Conversion graphs | - Plot and Interpret graphs arising from real situations such as distance-time and speed-time graphs <br> - Understand that the steeper the gradient the faster the object in a distance-time graph <br> - Use conversion graphs such as for exchange rates <br> - Recognise real life graphs for water depth problems with 3D shapes | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 2 test <br> - End of year assessments <br> - PQWC |
| Shape, Perimeter and Area | - Properties of quadrilaterals <br> - 3D shape vocabulary <br> - Plans and elevations <br> - Nets <br> - Units of measurement <br> - Area of 2D shapes <br> - Volume and surface area of cuboids <br> - Circle vocabulary <br> - Area and circumference of circles and part-circles | - Derive and apply properties of special types of quadrilaterals <br> - Know the meanings of faces, surfaces, edges and vertices and identify them in 3D shapes <br> - Recognise and draw 3D shapes from their plans and elevations <br> - Create plans and elevations for given 3D shapes <br> - Construct nets of 3D shapes <br> - Choose and use units of measurement to measure, estimate, calculate and solve problems in a range of contexts <br> - Know rough metric equivalents of imperial measures in everyday use and use given conversions to answer problems <br> - Know and use the formulae for the area of a triangle, parallelogram and trapezium | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 3 test <br> - End of year assessments <br> - PQWC |


|  |  | - Find the volume and surface area of cuboids or 3D shapes formed of cuboids <br> - Construct equations to solve cuboid volume and surface area problems <br> - Understand circle vocabulary such as radius, diameter, circumference, arc, sector, chord, and segment <br> - Know and use the formulae for the circumference and area of a circle, and use these to answer problems relating to shapes that contain semicircles and quarter-circles |  |
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| Pythagoras' <br> Theorem | - Pythagoras' theorem <br> - Contextual problems | - Understand the hypotenuse is the side opposite the rightangle in a right-angled triangle <br> - Use Pythagoras' theorem to find missing sides in right-angled triangles including within contextual problems | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 3 test <br> - End of year assessments <br> - PQWC |
| Probability | - Simple probability <br> - Sample spaces <br> - Two-way tables <br> - Experimental data and relative frequency | - Identify all possible mutually exclusive outcomes of a single event and know and apply the fact that the sum of probabilities of all outcomes is 1 <br> - Know that, if the probability of an event occurring is $p$, then the probability of it not occurring 1-p <br> - Use diagrams and tables to record all possible mutually exclusive outcomes for single events and for two successive events, to include 2-way tables and sample spaces <br> - Know when to add or multiply two probabilities in simple situations <br> - Work out probabilities from two-way tables, including conditional probabilities and missing values <br> - Compare estimated experimental probabilities with theoretical probabilities, including relative frequencies <br> - Interpret results of an experiment using probability language and appreciate that random processes are unpredictable <br> - Estimate the number of times an event will occur, given the probability and the number of trials | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of module 3 test <br> - End of year assessments <br> - PQWC |


| Sequences | - Function machines <br> - Sequences and nth term | - Use functions machines and use brackets to represent the output of a function machine as an algebraic expression <br> - Generate linear sequences using term-to-term \& position-toterm rules <br> - Find the nth term of an arithmetic sequence including from diagrams <br> - Recognise and generate special sequences including those for odd, even, triangular, square, cube numbers and Fibonaccitype sequences, and powers of 2 | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of year assessments <br> - PQWC |
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| Straight Line Graphs | - Plot straight line graphs <br> - Find equations of lines | - Plot graphs of linear functions where $y$ is given explicitly in terms of $x$ <br> - Find the equation of a line given the graph <br> - Understand ' $m$ ' and ' $c$ ' in the context of graphs of straight lines <br> - Use straight line graphs to solve contextual problems | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of year assessments <br> - PQWC |
| Transformations | - Congruent and similar shapes <br> - Symmetry <br> - Reflection <br> - Translation <br> - Rotation <br> - Enlargement <br> - Invariance | - Identify congruent and similar shapes <br> - Identify rotational and reflective symmetry in 2-D shapes <br> - Reflect shapes in axes and lines such as $x=c, y=c, y=x, y=-x$ <br> - Translate shapes using vectors <br> - Rotate shapes around points with angles that are multiples of $90^{\circ}$ <br> - Enlarge shapes from a point given positive integer scale factors <br> - Describe translations using the information above <br> - Understand the word invariant and identify numbers of invariant points for transformations | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - End of year assessments <br> - PQWC |
| Statistics | - Types of data <br> - Pie charts <br> - Stem and leaf diagrams <br> - Two-way tables <br> - Frequency diagrams <br> - Averages and range <br> - Comparing data | - Understand the differences between qualitative and quantitative data, and discrete and continuous data <br> - Construct and interpret pie charts <br> - Construct and interpret stem and leaf diagrams <br> - Plan, construct and interpret two-way tables for recording data <br> - Construct and interpret frequency diagrams | - Fluency and mastery homework <br> - Teacher assessment during lesson <br> - Year 8 module 1 assessment <br> - PQWC |


|  |  | - Calculate the mean, median, mode and range for discrete data <br> - Compare two simple distributions using summary statistics or graphs <br> - Calculate possible values of the set of data given summary statistics |  |
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| Number calculations | - Calculations <br> - Powers, roots and indices <br> - Systematic Counting <br> - Prime factor decomposition <br> - HCF and LCM | - Understand and use equivalences between $0.1,1 / 10$ and $10^{-1}$, and multiply and divide by any integer power of 10 <br> - Use given number facts to find the answer to another <br> - Be able to find square roots and cube roots by factorising <br> - Apply systematic listing strategies inc. use of the product rule for counting <br> - Prime factor decomposition using factor trees <br> - Find highest common factors and lowest common multiples of pairs or groups of numbers using prime factorisation and other methods, and apply this skill to contextual problems | - Year 8 Module 1 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Ratio, proportion <br> \& rates of change | - Using, understanding and applying ratio notation <br> - Proportion <br> - Compound measures <br> - Unit conversion | - Use ratio notation, including reduction to simplest form and 3-part ratios <br> - Divide a given quantity into two parts in a given part:part or part:whole ratio; express the division of a quantity into two parts as a ratio; apply ratio to real contexts and problems (such as those involving conversion, comparison, scaling, mixing, concentrations) <br> - Express multiplicative relationship between 2 quantities as ratio/fraction <br> - Understand and use proportion as equality of ratios <br> - Relate ratios to fractions and to linear functions <br> - Use the unitary method to solve simple word problems involving ratio and direct proportion <br> - Represent direct proportion graphically <br> - Understand and use density, speed or pressure to solve problems involving constant or average rates of change | - Year 8 Module 1 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |


|  |  | - Change freely between related standard units (e.g. time, length, area, volume/capacity, mass) and compound units (e.g. speed, rates of pay, prices, density, pressure) in numerical and algebraic contexts <br> - Calculate average speed, distance, time in mph and metric units and convert between metric speed measures |  |
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| Angles | - Angles in polygons <br> - Angles of parallel lines | - Find and use interior and exterior angles in both regular and irregular polygons <br> - Know and use properties of angles, parallel and intersecting lines, polygons <br> - Solve geometric problems involving angles | - Year 8 Module 1 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Algebra | - Algebraic Fractions <br> - Substitution <br> - Changing the subject <br> - Linear equations <br> - Trial \& Improvement | - $+,-, x, \div$ and simplify algebraic fractions where numerator and denominator are single terms <br> - Substitute numbers into expressions and formula <br> - change the subject of a formula <br> - Construct and solve multi-step linear equations with integer coefficients <br> - Use systematic trial and improvement methods and ICT tools to find approximate solutions of equations | - Year 8 Module 2 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Inequalities | - Inequalities on a Number Line <br> - Solving Inequalities <br> - Set Notation | - Representing inequalities on a number line <br> - Write down whole number values that satisfy an inequality <br> - Solve linear inequalities in one variable <br> - Solve two simultaneous linear inequalities algebraically <br> - Represent the solution set for inequalities using set notation <br> - Use inequality notation to specify simple error intervals due to truncation or rounding | - Year 8 Module 2 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Bearings and scale drawing | - Bearings <br> - Scale drawing | - Use bearings to specify direction <br> - Give a bearing between the points on a map or scaled plan <br> - Given the bearing of $A$ from $B$, work out the bearing of $B$ from A <br> - Mark on a diagram the position of B given its bearing from $A$ | - Year 8 Module 2 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |


|  |  | - Read and construct scale drawings <br> - Use and interpret maps and scale drawings, using a variety of scales and units and using proper map scales (1:25000) <br> - Use and interpret scale drawings, where scales use mixed units, and drawings aren't done on squared paper, but have measurements marked on them. |  |
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|  <br> Measures | - Coordinate geometry | - Find the length of a line segment <br> - Find the coordinates of a mid-point of a line <br> - Solve geometrical problems on coordinate axes | - Year 8 Module 2 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Equations of lines | - Plot graphs of linear functions <br> - Equations of straight lines <br> - Simultaneous equations | - Generate points and plot graphs of linear functions <br> - Recognise that linear functions can be rearranged to give $y$ explicitly in terms of $x$ <br> - Know that the gradient of a line is the change in y over change in x . <br> - Use gradients to interpret how one variable changes in relation to another <br> - Find the gradient of lines given by equations of the form $y=$ $m x+c$ and $a x+b y=c$ <br> - Find the equation of a straight line from its graph <br> - Parallel lines | - Year 8 Module 3 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Area and volume | - Conversion between measures <br> - Surface area \& Volume | - Convert between area measures and between volume measures <br> - Calculate the surface area and volume of right prisms (including the use of Pythagoras Theorem to calculate missing sides in triangular prisms when calculating surface area and volume) <br> - Calculate the lengths and areas given the volumes in right prisms | - Year 8 Module 3 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |


| Simultaneous equations | - Simultaneous equations | - Solve a pair of simultaneous linear equations by eliminating one variable and by linking a graph of the equations to the algebraic solution <br> - Solve simultaneous linear equations by substitution <br> - Consider cases of simultaneous linear equations that have no solution or an infinite number of solutions <br> - Construct and solve simultaneous equations | - Year 8 Module 3 Test <br> - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
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| Trigonometry | - Trigonometry with right angled triangles <br> - Trigonometric exact values | - Understand and use trigonometric relationships in right-angled triangles, and use these to solve problems (including bearings and angle of elevation and depressions) <br> - Use the trigonometric keys of a calculator <br> - Exact values and surds for trig functions: Know the exact values of $\sin \theta$ and $\cos \theta$ for $\theta=0^{\circ}, 30^{\circ}, 45^{\circ}, 60^{\circ}$ and $90^{\circ}$; know the exact value of $\tan \theta$ for $\theta=0^{\circ}, 30^{\circ}, 45^{\circ}$ and 60 | - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Fractions and percentages | - Percentages \& Fractions <br> - Multiple percentage/proportion change | - Interpret percentages and percentage changes as a fraction or a decimal, and interpret these multiplicatively <br> - Express one quantity as a percentage of another <br> - Compare two quantities using percentages, including a range of calculations and contexts <br> - Work with percentages greater than $100 \%$ <br> - Find a percentage of a quantity using a multiplier <br> - Solve problems involving percentage change, including percentage increase/decrease (using a multiplier and other methods) and original value problems <br> - Use percentages in real-life situations: VAT, value of profit or loss, simple interest, income tax calculations <br> - Use compound interest <br> - Represent repeated proportional change using a multiplier raised to a power <br> - Use percentages in real-life situations: compound interest, depreciation, percentage profit and loss <br> - Calculate repeated proportional change | - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |


|  |  | - Express one quantity as a fraction of another, where the fraction is greater than 1 |  |
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| Constructions | - Constructions | - (Including to and from a point \& including knowing the perpendicular is the shortest distance from a point to a line), angular bisectors \& triangles <br> - Construct angles of $60^{\circ}, 90^{\circ}, 30^{\circ}, 45^{\circ}$ | - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Venn diagrams and set notation | - Introduction to sets | - Set notation \& definitions <br> - Venn Diagram <br> - Union \& intersection of sets | - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |
| Algebraic manipulation | - Quadratics <br> - Identities <br> - Algebraic Proof | - Expand and simplify double brackets <br> - Square a linear expression and collect like terms <br> - expand product of two or more linear expressions of form $\mathrm{ax} \pm$ b <br> - Factorise and solve quadratic expressions of the form $x^{2}+b x+$ c , including the difference of two squares <br> - Introduce factorising and solving quadratics equations of the form $\mathrm{ax}^{2}+\mathrm{bx}+\mathrm{c}$ where $\mathrm{a}>1$ <br> - Algebraic identities <br> - Answer simple proof and 'show that' questions using consecutive integers $(n, n+1)$, squares $a^{2}, b^{2}$, even numbers $2 n$, and odd numbers $2 n+1$ | - In class teacher assessment <br> - Fluency \& Mastery Homework <br> - End of year exams |

